

# Misusing Misuse-Resistance in APE

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DIAC 2014, Santa Barbara, USA



# Nonce-based Encryption

- Formalized by Rogaway
- Primary Condition
  - *Uniqueness* of the nonce in every instantiation of the cipher
- Interesting Consequence
  - Automatic protection from Differential Fault Analysis (DFA)
- DFA assumption
  - Ability to induce faults in the intermediate state of the cipher while replaying the encryption with the same plaintext.
  - No longer holds due to introduction of nonce

# Misuse-Resistance

- A desirable property for authenticated ciphers.
- Avoids maintaining a nonce-generator
- Suited for resource constrained environments
- Addressed in CAESAR selection portfolio
- However, there is some collateral damage.
  - Nonce assumption no longer holds
  - Opens up the ciphers for DFA
- This work explores this idea to mount efficient DFA on misuse-resistant AE scheme APE

# APE

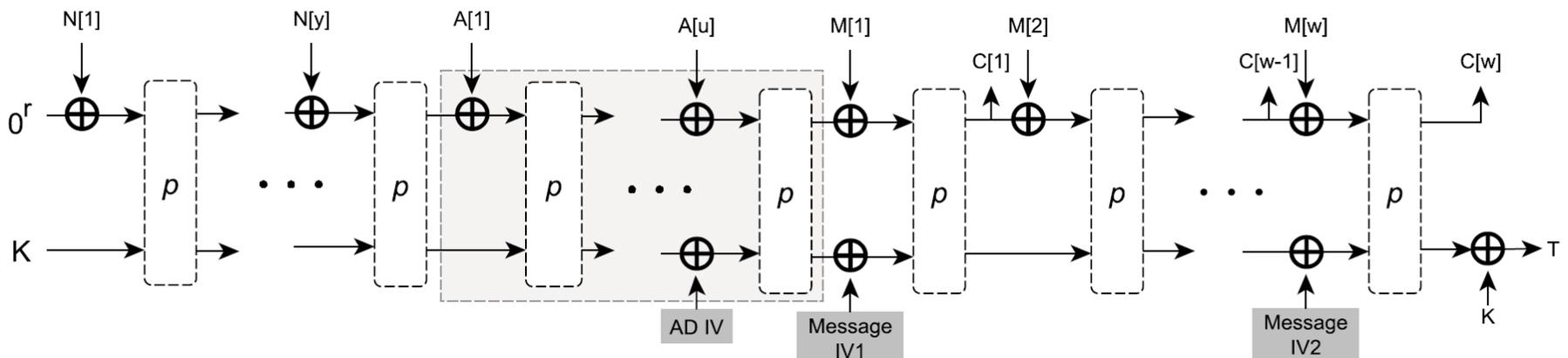
- Authenticated Permutation-based Encryption – APE
  - Introduced first in FSE 2014
  - First misuse-resistant permutation-based AE scheme
  - Inspired from SPONGE
  - Targeted for lightweight environments
  - Basically a mode of operation
  - Can be instantiated with permutations of hashes like SPONGENT/QUARK/PHOTON
- Reintroduced in CAESAR
  - Along with HANUMAN & GIBBON
  - Part of PRIMATES family of authenticated ciphers
  - Now with new indigenous permutation called PRIMATE

# The PRIMATE Permutation

- Internal permutation for APE/HANUMAN/GIBBON
  - Inspired from FIDES authenticated cipher
  - Structurally follows AES round function
- Has two variants
  - PRIMATE-80/120
  - Internal state realized as  $(5 \times 8) / (7 \times 8)$  five-bit elements
- Component Transformations
  - SubBytes
  - ShiftRows
  - MixColumns
  - Round constant addition

# PRIMATE-APE

- $N[\cdot]$  – Nonce block
- $A[\cdot]$  – Associated data block
- $M[\cdot]$  – message block
- $K$  – Key (160 bit for APE-80)
- The IVs are predefined and vary according to the nature of the length of message and associated data.
- This work uses APE-80 (can be extended to APE-120)



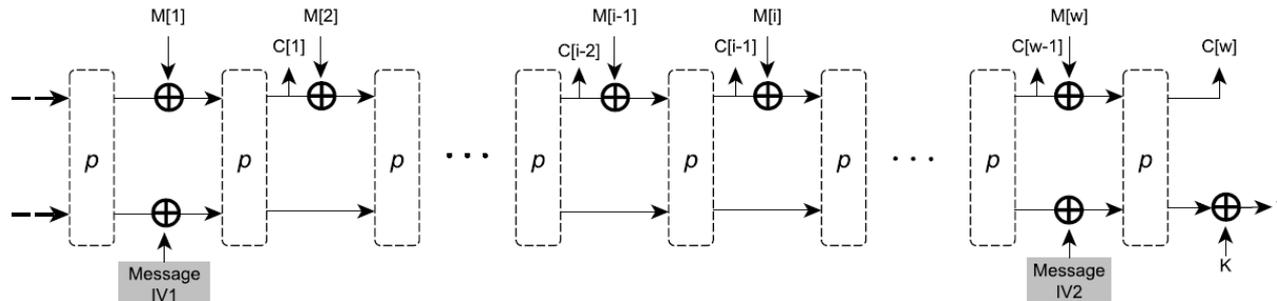
# Misusing Misuse-Resistance

- Concept of faulty collisions :
  - Not a real collision
  - Attacker induces a fault in the state of the cipher so that two different plaintexts produce the same tag.
- Idea : To find faulty collisions
  - Feasible due to misuse-resistance
    - **Observation:** APE is misuse-resistant up to a common prefix.
- Common prefix implication:
  - Plaintexts can be of the following form:
    - $M1 = x_0 || x_1 || x_2 || \dots || \mathbf{x}_i || \dots || x_w$
    - $M2 = x_0 || x_1 || x_2 || \dots || \mathbf{x}'_i || \dots || x_w$

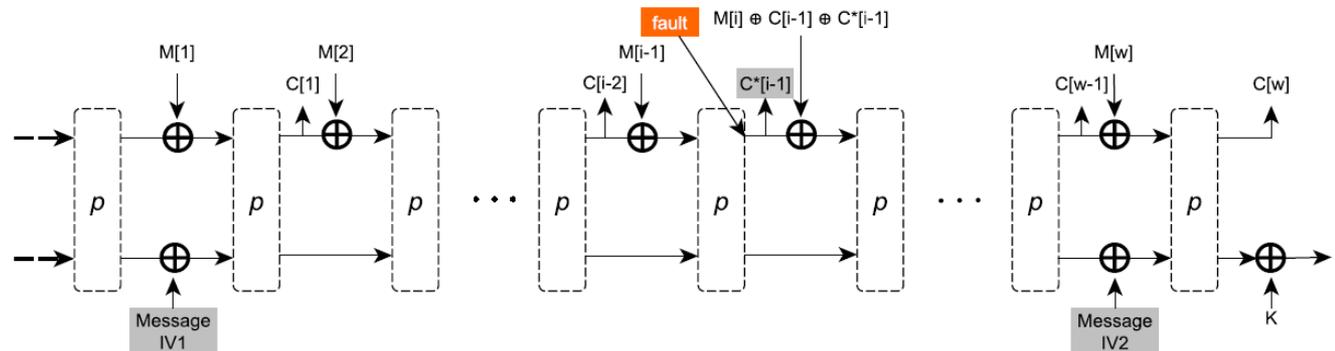
# A Faulty Collision

- Exploits : Misuse-resistance + Online nature
  - Induce random word fault in  $(i-1)^{\text{th}}$  ciphertext output
  - Observe faulty  $(i-1)^{\text{th}}$  output & manipulate  $i^{\text{th}}$  message input

Plaintext1 = M[1] || M[2] || ... || M[i] || M[i+1] || ... || M[w]  
 Ciphertext1 = C[1] || C[2] || ... || C[i] || C[i+1] || ... || C[w]  
 Tag = T



Plaintext2 = M[1] || M[2] || ... || M[i-1] || (M[i]  $\oplus$  C[i-1]  $\oplus$  C\*[i-1]) || M[i+2] || ... || M[w]  
 Ciphertext2 = C[1] || C[2] || ... || C\*[i-1] || C[i] || ... || C[w]  
 Tag = T

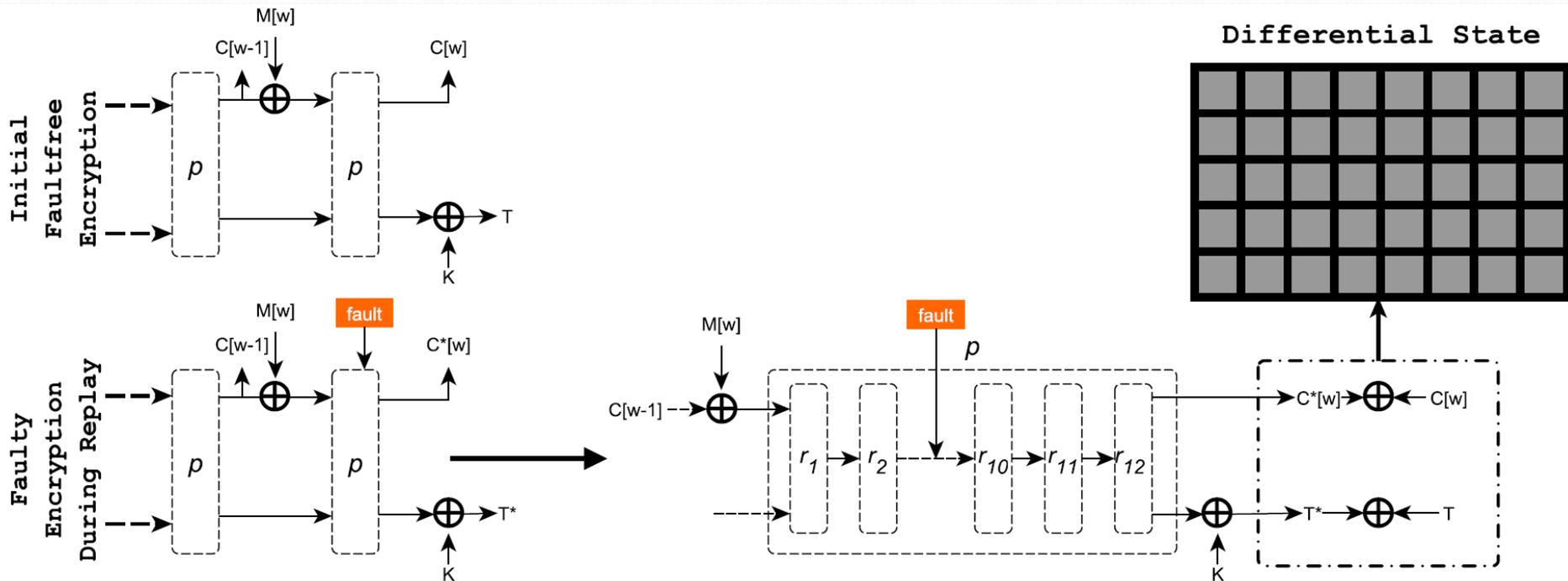


# Implications of a Faulty Collision

- Ability to replay the encryption
- Recall
  - This is one of the fundamental requirements to mount differential fault analysis attacks
- Next, we explore the prospect of DFA in the presence of faulty collisions
- Fault model assumed is random word fault
  - Recall : word in case of APE is a 5-bit vector

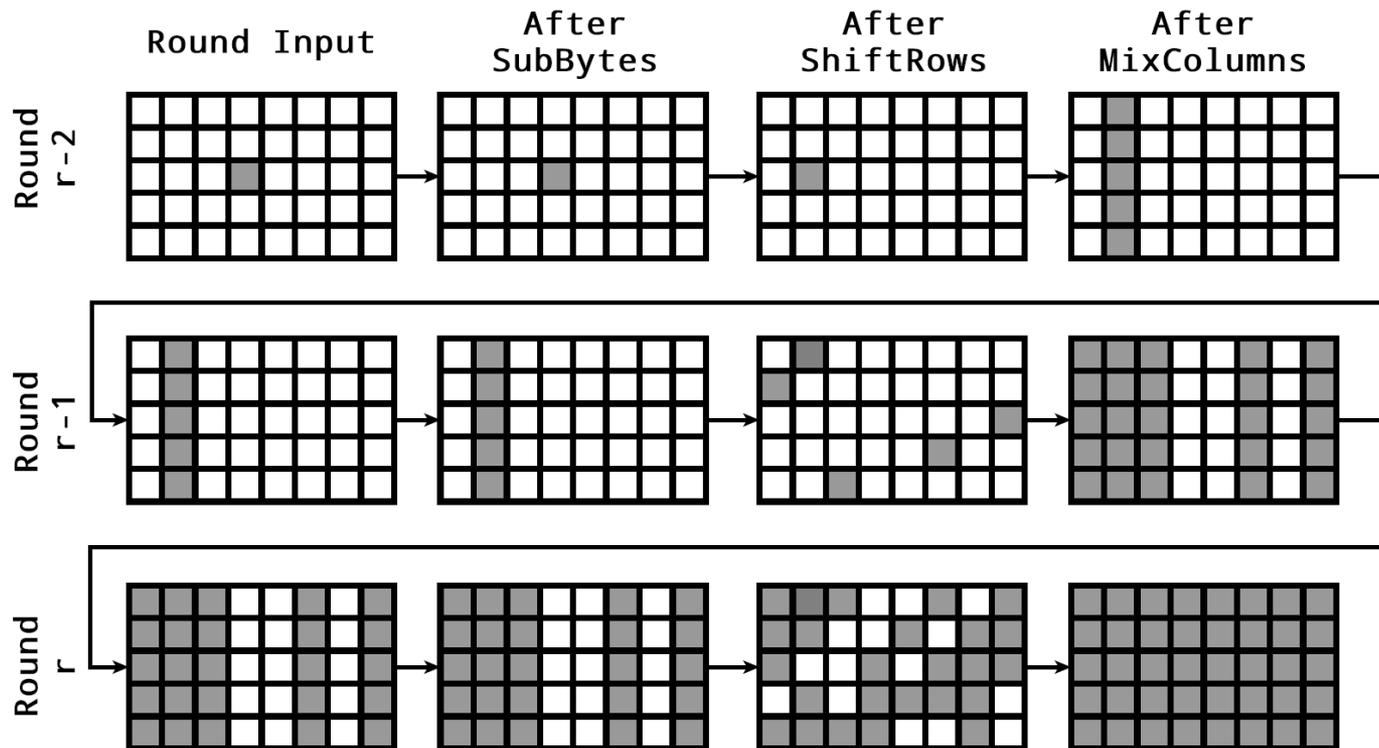
# Fault Induction

- Fault induced at the input of 10<sup>th</sup> round of the final iteration of APE
- Next study the fault diffusion in the differential state in the remaining rounds



# Fault Diffusion

- Observe: Exactly 3 specific unaffected columns at the start of  $r^{\text{th}}$  round due to diagonal word fault at the start of  $(r-2)^{\text{th}}$  round.
  - Helps to identify fault source diagonal by observing differential state
  - Exploits the non-square nature of state matrix

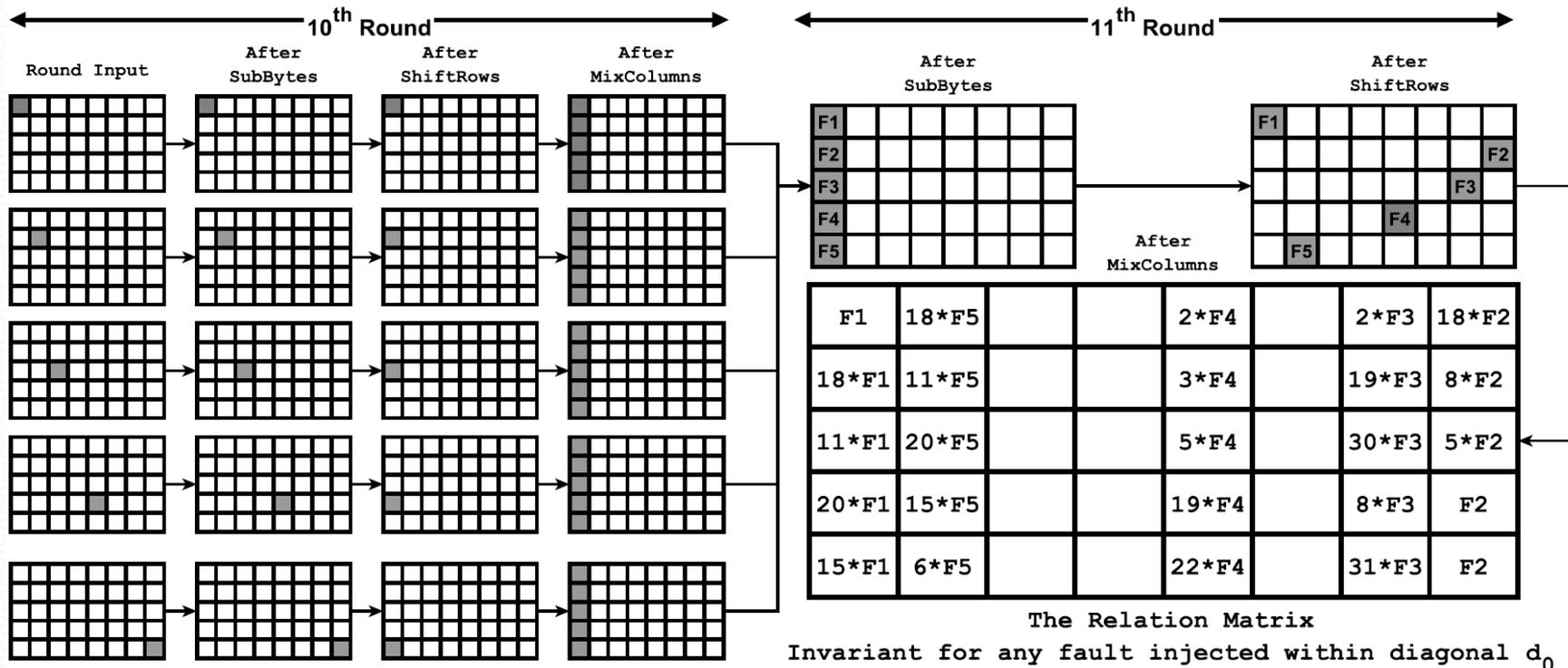


# Diagonal Fault Analysis

- Advanced differential fault attack
  - Introduced in 2009, specially suited for AES-like constructions
  - Has been highlighted in the book *Fault Analysis in Cryptography* as one of the most efficient DFA on AES
    - Available on Eprint archive - <https://eprint.iacr.org/2009/581>
  - Exploits equivalence of fault induced in the same diagonal of the state matrix
- Can be applied on APE
  - But not directly
  - Last round MixColumn inclusion - major deviation from AES
  - Makes classical diagonal attack inefficient
  - Need some adaptation
    - Focus on recovering the state instead of the key

# The Fault Invariant

- The diagonal principle :
  - *Equivalence of faults limited to a diagonal*
- The relation matrix is governed by MixColumns



EscApe :

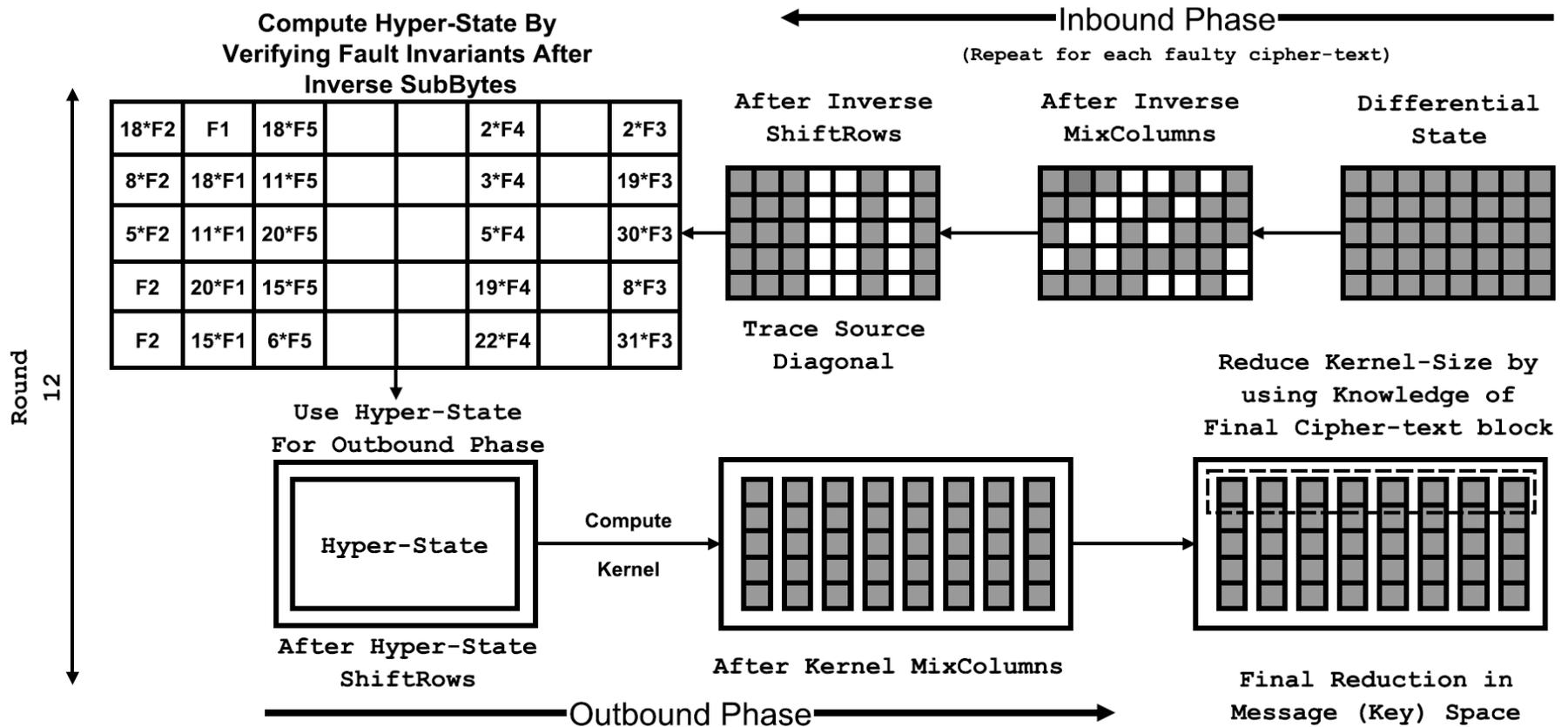
# Diagonal Fault Analysis of APE

- Inbound phase
  - Invert the differential state (computed from correct and faulty output) to reach up to state after last round SubBytes.
  - Use unaffected columns to identify source fault diagonal and load appropriate relation matrix
  - Solve equations involving fault invariant to generate hyper-state
  - Hyper-State is a special structure where every element is a set of candidates computed after equation solving
    - Helps capture the notion of candidate states for the correct state

# EscApe (contd.)

- The Outbound phase
  - Apply ShiftRows to Hyper-state
  - Compute Kernel (Refer paper for details)
  - Apply MixColumns to Kernel
- Reduce message space by verifying candidates against last ciphertext block
  - Exploits the availability of last ciphertext block
  - Simulations confirm large-scale reduction due to this
- Reduced message space directly corresponds to reduced key space.

# EscApe :The Final Picture



# Results

- In the presence of faulty collision:

| <b>Fault Count</b> | <b>Fault Type</b>   | <b>Avg. Final Key Space</b> |
|--------------------|---|-----------------------------|
| 1                  | Random word fault at the start of 10 <sup>th</sup> round in the last iteration of APE | $2^{80}$                    |
| 2                  |   | $2^{25}$                    |
| 3                  |   | $2^5$                       |
| 4                  |   | 1                           |

# Epilogue

- Shown how the desirable property of misuse-resistance becomes the gateway for DFA
- First fault analysis of SPONGE when used in the context of authenticated encryption
- EscApe : efficient diagonal attack on APE
  - 2 faults lead to a practical attack, 4 give the unique key
- Removal of final truncation of FIDES in APE makes EscApe highly efficient
- Finally, its evident that
  - Misuse-resistance,
  - Design of underlying permutation and
  - Choice of mode of operationcan all contribute to the susceptibility of authenticated ciphers to fault attacks

# Thank You

- Please forward any queries to  
**crypto@dhimans.in**
- Full version of the paper :  
**<http://de.ci.phe.red>**  
**or, CAESAR mailing list**

